

Opener

If $\frac{dy}{dx} = 2y^2$ and if $y = -1$ when $x = 1$, then when $x = 2$, $y =$

(A) $-\frac{2}{3}$

(B) $-\frac{1}{3}$

(C) 0

(D) $\frac{1}{3}$

(E) $\frac{2}{3}$

6-1 day 2 Differential Equations and
slope fields

$$\frac{1}{2}y^2 dy = 1 dx \quad -\frac{1}{2}y^{-1} = x + C \quad y^{-1} = -2x + C$$

$$y^{-1} = \frac{1}{2x+C} \quad C=1 \quad x = \frac{1}{-2x+C}$$

$$y = \frac{1}{2x+1} \quad y = -\frac{1}{2x+1} \quad x = -\frac{1}{4y+1} \quad y = \frac{1}{3}$$

6-1 day 2 Differential Equations and Slope Fields

Learning Objectives:

I can graph and interpret a slope field for a given differential equation

Ex2. Solve

$$\frac{dy}{dx} = x + y$$

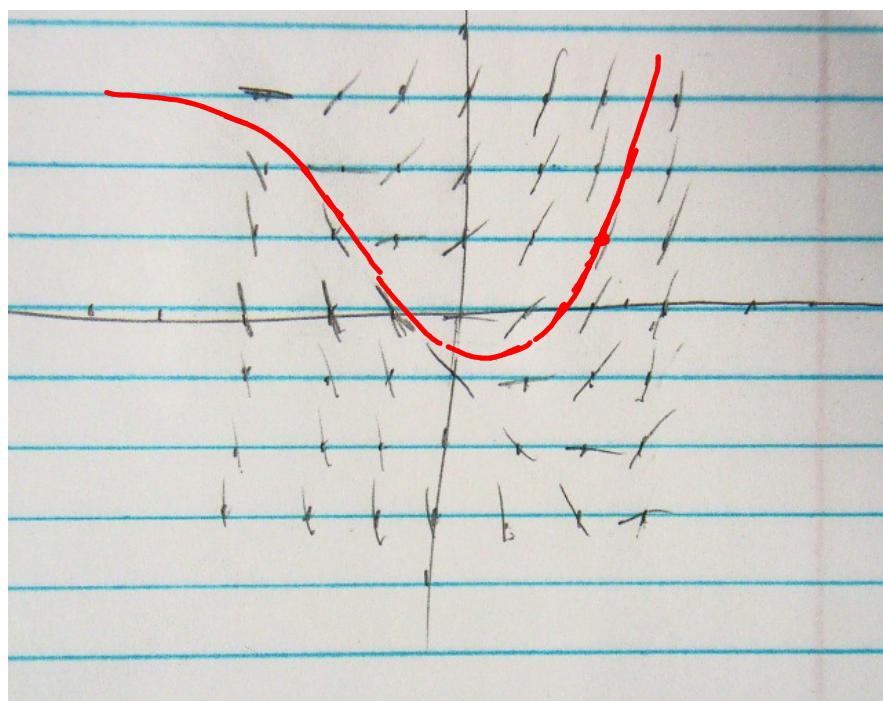
$$dy = (x+y) dx$$

$$dy = x dx + y dx$$

$$dy - y dx = dx$$

Non-Sep Diffy Q

$$\frac{dy}{dx} = x + y$$



Ex3. Sketch the slope field for the given differential equation. Then solve the differential equation

$$\frac{dy}{dx} = \frac{x}{y^2}$$

$$\begin{aligned} dy &= \frac{x}{y^2} dx \\ y^2 dy &= x dx \\ \frac{1}{3} y^3 &= \frac{1}{2} x^2 + C \\ y &= \sqrt[3]{\frac{3}{2} x^2 + C} \end{aligned}$$

(0, 1)

$$\begin{aligned} 1 &= \sqrt[3]{\frac{3}{2}(0)^2 + C} \\ 1 &= \sqrt[3]{C} \\ C &= 1 \end{aligned}$$

$$y = \sqrt[3]{\frac{3}{2}x^2 + 1}$$

(-1, 0)

$$\begin{aligned} 0 &= \sqrt[3]{\frac{3}{2}(-1)^2 + C} \\ 0 &= \sqrt[3]{\frac{3}{2} + C} \end{aligned}$$

$$0 = \frac{3}{2} + C$$

$$-\frac{3}{2} = C$$

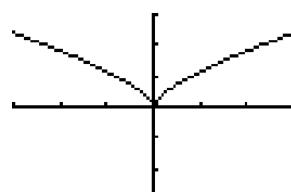
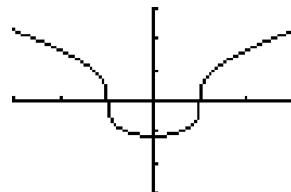
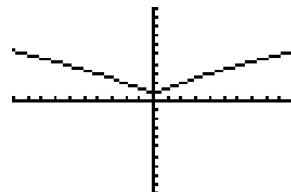
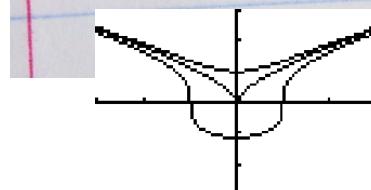
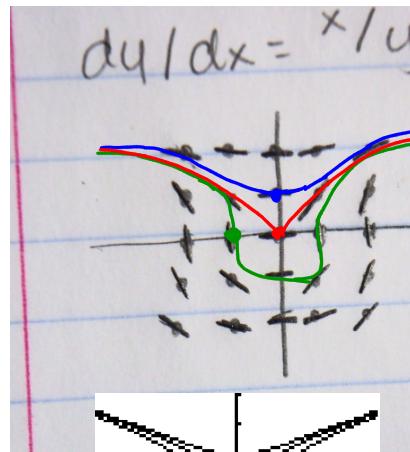
$$y = \sqrt[3]{\frac{3}{2}x^2 - \frac{3}{2}}$$

(0, 0)

$$0 = \sqrt[3]{\frac{3}{2}(0)^2 + C}$$

$$0 = C$$

$$y = \sqrt[3]{\frac{3}{2}x^2}$$



Ex4. Solve the differential equation

$$\frac{dy}{dx} = yx \quad \text{initial condition } (0,2)$$

$$\frac{1}{y} dy = x dx \quad \ln|y| = \frac{1}{2}x^2 + C$$

$$y = e^{\frac{1}{2}x^2 + C} \quad z = e^{\frac{1}{2}0^2 + C}$$

$$z = e^C \quad \ln z = C$$

$$y = e^{\frac{1}{2}x^2 + \ln z}$$

$$y = e^{\frac{1}{2}x^2} \cdot e^{\ln z}$$

$$y = 2e^{\frac{1}{2}x^2}$$

Homework

pg 328 #29-40, 49, 50, 55, 57,
58, 61, 62, 64